

<<椭圆函数>>

图书基本信息

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作者：S.Lang

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## 内容概要

Elliptic functions parametrize elliptic curves, and the intermingling of the analytic and algebraic-arithmic theory has been at the center of mathematics since the early part of the nineteenth century. Some new techniques and outlooks have recently appeared on these old subjects, continuing in the tradition of Kronecker, Weber, Fricke, Hasse, Deuring. Shimura's book Introduction to the arithmetic theory of automorphic functions is a splendid modern reference, which I found very helpful myself to learn some aspects of elliptic curves. It emphasizes the direction of the Hasse-Weil zeta function, Hecke operators, and the generalizations due to him to the higher dimensional case (abelian varieties, curves of higher genus coming from an arithmetic group operating on the upper half plane, bounded symmetric domains with a discrete arithmetic group whose quotient is algebraic). I refer the interested reader to his book and the bibliography therein.

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书籍目录

PART ONEccGENERAL THEORY Chapter1 Elliptic Functions 1 The Liouville Theorems 2 The Weierstrass Function 3 The Addition Theorem 4 Isomorphism Classes of Elliptic Curves 5 Endomorphisms and Automorphisms Chapter2 Homomorphisms 1 Points of Finite Order 2 Isogenies 3 The Involution Chapter 3 The Modular Function 1 The Modular Group 2 Automorphic Functions of Degree  $2k$  3 The Modular Function  $j$  Chapter 4 Fourier Expansions 1 Expansion for  $G_k, c_2, c_3, c_4$  2 Expansion for the Weierstrass Function 3 Bernoulli Numbers Chapter 5 The Modular Equation 1 Integral Matrices with Positive Determinant 2 The Modular Equation 3 Relations with Isogenies Chapter 6 Higher Levels 1 Congruence Subgroups 2 The Field of Modular Functions Over  $\mathbb{C}$  3 The Field of Modular Functions Over  $\mathbb{Q}$  4 Subfields of the Modular Function Field Chapter 7 Automorphisms of the Modular Function Field 1 Rational Adeles of  $GL_2$  2 Operation of the Rational Adeles on the Modular Function Field 3 The Shimura Exact Sequence

PART TWOccCOMPLEX MULTIPLICATION

ELLIPTIC CURVES WITH SINGULAR INVARIANTS Chapter 8 Results from Algebraic Number Theory 1 Lattices in Quadratic Fields 2 Completions 3 The Decomposition Group and Frobenius Automorphism 4 Summary of Class Field Theory Chapter 9 Reduction of Elliptic Curves 1 Non-degenerate Reduction, General Case 2 Reduction of Homomorphisms 3 Coverings of Level  $N$  4 Reduction of Differential Forms Chapter 10 Complex Multiplication 1 Generation of Class Fields, Deuring's Approach 2 Idelic Formulation for Arbitrary Lattices 3 Generation of Class Fields by Singular Values of Modular Functions 4 The Frobenius Endomorphism Appendix A Relation of Kronecker Chapter 11 Shimura's Reciprocity Law 1 Relation Between Generic and Special Extensions 2 Application to Quotients of Modular Forms Chapter 12 The Function  $(a, t) / (t)$  1 Behavior Under the Artin Automorphism 2 Prime Factorization of its Values 3 Analytic Proof for the Congruence Relation of  $f_j$

Chapter 13 The  $l$ -adic and  $p$ -adic Representations of Deuring 1 The  $l$ -adic Spaces 2 Representations in Characteristic  $p$  3 Representations and Isogenies 4 Reduction of the Ring of Endomorphisms 5 The Deuring Lifting Theorem Chapter 14 Ihara's Theory 1. Deuring Representatives 2 The Generic Situation 3 Special Situations

PART THREE ELLIPTIC CURVES WITH NON-INTEGRAL INVARIANT Chapter 15 The Tate Parametrization 1 Elliptic Curves with Non-integral Invariants 2 Elliptic Curves Over a Complete Local Ring Chapter 16 The Isogeny Theorems 1 The Galois  $p$ -adic Representations 2 Results of Kummer Theory 3 The Local Isogeny Theorems 4 Supersingular Reduction 5 The Global Isogeny Theorems Chapter 17 Division Points Over Number Fields 1 A Theorem of Shafarevich 2 The Irreducibility Theorem 3 The Horizontal Galois Group 4 The Vertical Galois Group 5 End of the Proof

PART FOURccTHE TATE FUNCTION AND KRONECKER LIMIT FORMULA Chapter 18 Product Expansions 1 The Sigma and Zeta Function Appendix The Skew Symmetric Pairing 2 A Normalization and the  $q$ -product for the  $a$ -function 3  $q$ -expansions Again 4 The  $q$ -product for  $A$  5 The Eta Function of Dedekind 6 Modular Functions of Level  $2$  Chapter 19 The Siegel Functions and Klein Forms 1 The Klein Forms 2 The Siegel Functions 3 Special Values of the Siegel Functions Chapter 20 The Kronecker Limit Formulas 1 The Poisson Summation Formula 2 Examples 3 The Function  $K_s(x)$  4 The Kronecker First Limit Formula 5 The Kronecker Second Limit Formula Chapter 21 The First Limit Formula and  $L$ -series 1 Relation with  $L$ -series 2 The Frobenius Determinant 3 Application to the  $L$ -series Chapter 22 The Second Limit Formula and  $L$ -series 1 Gauss Sums 2 An Expression for the  $L$ -series

APPENDICES ELLIPTIC CURVES IN CHARACTERISTIC  $p$  Appendix 1 Algebraic Formulas in Arbitrary Characteristic BY J. TATE 1 Generalized Weierstrass Form 2 Canonical Forms 3 Expansion Near  $O$ ; The Formal Group Appendix 2 The Trace of Frobenius and the Differential of First Kind 1 The Trace of Frobenius 2 Duality 3 The Tate Trace 4 The Cartier Operator 5 The Hasse Invariant Bibliography Index

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