

<<拟微分算子技巧>>

图书基本信息

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### 内容概要

It is generally well known that the Fourier-Laplace transform converts a linear constant coefficient PDE  $P(D)u=f$  on  $\mathbb{R}^n$  to an equation  $P(\xi)u(\xi)=f(\xi)$ , for the transforms  $u, f$  of  $u$  and  $f$ , so that solving  $P(D)u=f$  just amounts to division by the polynomial  $P(\xi)$ . The practical application was suspect, and ill understood, however, until theory of distributions provided a basis for a logically consistent theory. Thereafter it became the Fourier-Laplace method for solving initial-boundary problems for standard PDE. We recall these facts in some detail in sections 1-4 of ch.0.

## &lt;&lt;拟微分算子技巧&gt;&gt;

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